

Answer Key 3

1.4: 10, 12, 18, 24, 25, 31, 47, 54, 65, 81, 86

1.5: 11, 20, 30, 41, 45, 51, 58, 70, 73, 76, 90, 93, 109, 127, 139

1.4

<p>10) Since the denominator is $3t+6$, Domain = $\{t \mid t \in \mathbb{R}, t \neq -2\}$</p>	<p>12) Since the denominator is $\sqrt{x-1}$ $\{x \mid x \in \mathbb{R}, x > 1\}$</p>
<p>18) $\frac{x^2 - x - 2}{x^2 - 1} = \frac{(x-2)(x+1)}{(x-1)(x+1)} = \frac{x-2}{x-1}$</p>	<p>24) $\frac{1-x^2}{x^3-1} = \frac{(1-x)(1+x)}{(x-1)(x^2+x+1)} = \frac{-(x+1)}{x^2+x+1}$</p>
<p>25) $\frac{4x}{x^2-4} \cdot \frac{x+2}{16x} = \frac{x+2}{(x+2)(x-2)4} = \frac{1}{4(x-2)}$</p>	<p>31) $\frac{x^2+7x+12}{x^2+3x+2} \cdot \frac{x^2+5x+6}{x^2+6x+9} =$ $\frac{(x+3)(x+4)}{(x+1)(x+2)} \cdot \frac{(x+2)(x+3)}{(x+3)(x+3)} = \frac{x+4}{x+1}$</p>
<p>47) $u+1 + \frac{u}{u+1} = \frac{(u+1)^2 + u}{u+1} = \frac{u^2 + 3u + 1}{u+1}$</p>	<p>54) $\frac{x}{x^2+x-2} - \frac{2}{x^2-5x+4} =$ $\frac{x}{(x+2)(x-1)} - \frac{2}{(x-4)(x-1)} =$ $\frac{1}{x-1} \left[\frac{x}{x+2} - \frac{2}{x-4} \right] = \frac{1}{x-1} \left[\frac{x^2 - 4x - 2x - 4}{(x+1)(x-4)} \right] =$ $\frac{1}{x-1} \left[\frac{x^2 - 6x - 4}{(x+2)(x-4)} \right]$</p>
<p>65) $\frac{x - \frac{x}{y}}{y - \frac{y}{x}} = \frac{\frac{xy-x}{y}}{\frac{xy-y}{x}} = \frac{\frac{x(y-1)}{y}}{\frac{y(x-1)}{x}} =$ $\frac{x(y-1)}{y} \cdot \frac{x}{y(x-1)} = \frac{x^2(y-1)}{y^2(x-1)}$</p>	<p>81) $\frac{2(1+x)^{1/2} - x(1+x)^{-1/2}}{x+1} \cdot \frac{(1+x)^{1/2}}{(1+x)^{1/2}} =$ $\frac{2(1+x) - x}{(x+1)^{3/2}} = \frac{x+2}{(x+1)^{3/2}}$</p>
<p>86) $\frac{3}{2-\sqrt{5}} \cdot \frac{2+\sqrt{5}}{2+\sqrt{5}} = \frac{6+3\sqrt{5}}{4-5} = -6-3\sqrt{5}$</p>	

1.5: 11, 20, 30, 41, 45, 51, 58, 70, 73, 76, 90, 93, 109, 127, 139

<p>11) a) $\frac{1}{2} - \frac{1}{2-4} = \frac{1}{2} - \frac{-1}{2} = 1$ Yes! b) $\frac{1}{4} - \frac{1}{4-4} = \frac{1}{4} - \frac{1}{0}$ Undefined so No!</p>	<p>20) $\left(\frac{2}{5}x - 1\right)10 = \left(\frac{3}{10}x + 3\right)10$ $4x - 10 = 3x + 30$ $x = 40$</p>
<p>30) $(\sqrt{3}x + \sqrt{12}) \cdot \sqrt{3} = \left(\frac{x+5}{\sqrt{3}}\right) \cdot \sqrt{3}$ $3x + \sqrt{36} = x + 5$ $2x = -1$ $x = -\frac{1}{2}$</p>	<p>41) $a^2 + b^2 = c^2$ $b = \pm\sqrt{c^2 - a^2}$</p>
<p>45) $x^2 + x - 12 = 0$ $(x-3)(x+4) = 0$ $x = \{3, -4\}$</p>	<p>51) $3x^2 + 5x = 2$ $3x^2 + 5x - 2 = 0$ $(3x-1)(x+2) = 0$ $x = \left\{\frac{1}{3}, -2\right\}$</p>
<p>58) $x^2 - 4x + 2 = 0$ $x^2 - 4x + 4 + 2 = 4$ $(x-2)^2 = 2$ $x - 2 = \pm\sqrt{2}$ $x = 2 \pm \sqrt{2}$</p>	<p>70) $3x^2 + 7x + 4 = 0$ $(3x+4)(x+1) = 0$ $x = \left\{-\frac{4}{3}, -1\right\}$</p>
<p>73) $9x^2 + 12x + 4 = 0$ $(3x+2)^2 = 4$ $x = \left\{-\frac{2}{3}\right\}$</p>	<p>76) $x^2 - 4x + 1 = 0$ $x^2 - 4x + 4 + 1 = 4$ $(x-2)^2 = 3$ $x - 2 = \pm\sqrt{3}$ $x = 2 \pm \sqrt{3}$</p>

<p>90)</p> $\left(\frac{x+5}{x-2}\right)(x^2-4) = \left(\frac{5}{x+2} + \frac{28}{x^2-4}\right)(x^2-4)$ $(x+5)(x+2) = 5(x-2) + 28$ $x^2 + 7x + 10 = 5x - 10 + 28$ $x^2 + 2x - 8 = 0$ $(x+4)(x-2) =$ $x = \{-4, 2\}$ <p>But note: 2 is not in the domain of either the original right or left expressions, so the only solution is -4</p>	<p>93)</p> $5 = \sqrt{4x-3}$ $25 = 4x-3$ $4x = 28$ $x = 7$ <p>Note it is important to check that</p> $5 = \sqrt{4 \cdot 7 - 3} = \sqrt{25} = 5$
<p>109)</p> $4(x+1)^{1/2} - 5(x+1)^{3/2} + (x+1)^{5/2} = 0$ $(x+1)^{1/2} [4 - 5(x+1) + (x+1)^2] = 0$ $(x+1)^{1/2} [4 - 5x - 5 + x^2 + 2x + 1] = 0$ $(x+1)^{1/2} [x^2 - 3x] = 0$ $x(x+1)^{1/2} (x-3) = 0$ $x = \{0, -1, 3\}$	<p>127)</p> $h = -16t^2 + h_0$ $0 = -16t^2 + 288$ $t^2 = \frac{288}{16} = 18$ $t = \pm\sqrt{18} = \pm 3\sqrt{2} \approx \pm 4.24$ <p>Note I approximate because this is a measurement.</p> <p>Also note the negative answer has no meaning so 4.24 seconds is the answer</p>
<p>139)</p> <p>The divide by x-1 step is illegitimate since x-1=0</p>	